

AP 4 Factorisation.

Factor commun.

$$\text{Ex 1) } ka + kb = k(a+b)$$

$$1) \text{ a) } 4x + xy = x(4+y)$$

$$\text{b) } 4(x+2) + (x+2)(1-3x) = (x+2)(4+1-3x) \\ = (x+2)(5-3x)$$

$$\text{c) } 7(x+4) + (x+4)(1-2x) = (x+4)(7+1-2x) \\ = (x+4)(8-2x)$$

$$2) \text{ a) } x^2 + xy = x(x+y)$$

$$\text{b) } (x+3)^2 + (x+3)(1-x) = (x+3)(x+3+1-x) \\ = (x+3)(4) = 4(x+3)$$

$$\text{c) } (2-x)^2 + (2-x)(1+2x) = (2-x)(2-x+1+2x) \\ = (2-x)(3+2x)$$

$$3) \text{ a) } 2xy + 3x = x(2y+3)$$

$$\text{b) } 2(x-4)(1+x) + 3(x-4) = (x-4)(2(1+x)+3) \\ = (x-4)(2+2x+3)$$

$$\text{c) } 5(x-2)(1-x) + 8(x-2) = (x-2)(5(1-x)+8) \\ = (x-2)(5-5x+8) \\ = (x-2)(13-5x)$$

$$\text{d) } 8x(x-1) + 5(x-1) = (x-1)(8x+5)$$

$$4) \text{ a) } 3x^2 + 5x = x(3x+5)$$

$$\text{b) } 3(1+x)^2 + 5(1+x) = (1+x)(3(1+x)+5) = (1+x)(8+3x)$$

$$\text{c) } -2(x-4)^2 + 3(x-4) = (x-4)(-2(x-4)+3) \\ = (x-4)(-2x+8+3) = (x-4)(-2x+11)$$

$$5) \text{ a) } xy + x = x(y+1)$$

$$\text{b) } (x-2)(1+x) + (x-2) = (x-2)(1+x+1) = (x-2)(2+x)$$

$$\text{c) } 5x(1-x) + (1-x) = (1-x)(5x+1)$$

$$\text{Ex 2) } ka - kb = k(a-b)$$

$$1) \text{ a) } 5x - xy = x(5-y)$$

$$\text{b) } 3(x+2) - (x+2)(1-x) = (x+2)(3-(1-x)) \\ = (x+2)(3-1+x) \\ = (x+2)(2+x) = (x+2)^2$$

$$\text{c) } 4(x+3) - (x+3)(1-2x) = (x+3)(4-(1-2x)) \\ = (x+3)(4-1+2x) \\ = (x+3)(3+2x)$$

$$2) \text{ a) } x^2 - xy = x(x-y)$$

$$\text{b) } (x-3)^2 - (x-3)(1-x) = (x-3)(x-3-(1-x)) \\ = (x-3)(x-3-1+x) \\ = (x-3)(2x-4)$$

$$\text{c) } (2-x)^2 - (2-x)(1+x) = (2-x)(2-x-(1+x)) \\ = (2-x)(2-x-1-x) \\ = (2-x)(1-2x)$$

$$3) \text{ a) } 3xy - 5x = x(3y-5)$$

$$\text{b) } 2(x+4)(1-x) - 2(x+4) = (x+4)(2(1-x)-2) \\ = (x+4)(2-2x-2) \\ = (x+4)(-2x) \\ = -2x(x+4)$$

$$\text{c) } 3(x-2)(1-x) - 4(x-2) = (x-2)(3(1-x)-4) \\ = (x-2)(3-3x-4) \\ = (x-2)(-1-3x)$$

$$\text{d) } -3x(x-1) - 2(x-1) = (x-1)(-3x-2)$$

$$4) \text{ a) } 5x^2 - 3x = x(5x-3)$$

$$\text{b) } 3(1+x)^2 - 2(1+x) = (1+x)(3(1+x)-2) \\ = (1+x)(3+3x-2) = (1+x)(1+3x)$$

$$\text{c) } -3(x-4)^2 - 2(x-4) = (x-4)(-3(x-4)-2) \\ = (x-4)(-3x+12-2) \\ = (x-4)(-3x+10)$$

$$5) \text{ a)} xy - x = x(y - 1)$$

$$\text{b)} (x-2)(1-2x) - (x-2) = (x-2)(1-2x-1)$$
$$= (x-2)(-2x)$$
$$= \boxed{-2x(x-2)}$$

$$\text{c)} x(1-x) - (1-x) = (1-x)(x-1)$$
$$= - (x-1)(x-1)$$
$$= \boxed{-(x-1)^2}$$